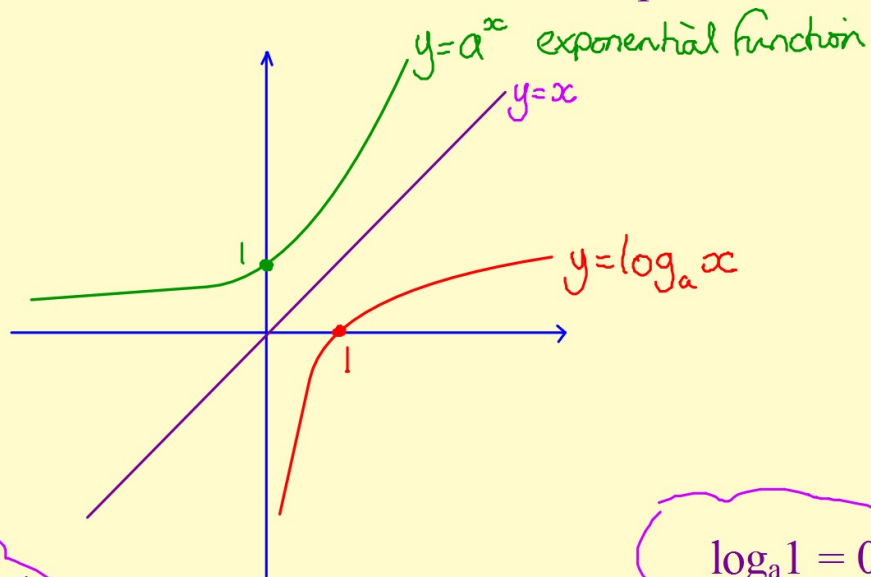


## Logarithmic & Exponential Functions

What you should already know:

The logarithmic function is the inverse of the exponential function.



$$\log_a a = 1$$
$$\log_3 3 = 1$$

$$\log_a 1 = 0$$
$$\log_3 1 = 0$$

Rules of Indices:

$$a^0 = 1$$

$$a^m \times a^n = a^{m+n}$$

$$\frac{a^m}{a^n} = a^{m-n}$$

$$a^1 = a$$

$$(a^p)^q = a^{pq}$$

$$a^{-1} = \frac{1}{a}$$

$$a^{\frac{1}{2}} = \sqrt{a}$$

$$\sqrt{a} \times \sqrt{a} = a^{\frac{1}{2}} \times a^{\frac{1}{2}} = a^{\frac{1}{2} + \frac{1}{2}} = a^1 = a$$

$$a^{\frac{m}{n}} = \sqrt[n]{a^m}$$

$$a^{-\frac{m}{n}} = \frac{1}{a^{\frac{m}{n}}} = \frac{1}{\sqrt[n]{a^m}}$$

## Converting Between Log and Exponential

$$y = a^x \quad \log_a y = \log_a a^x = x$$

$$9 = 3^x \quad \log_3 9 = \log_3 3^2 = 2$$

$$16 = 2^x \quad \log_2 16 = \log_2 2^4 = 4$$

$$32 = 2^x \quad \log_2 32 = \log_2 2^5 = 5$$

$$81 = 3^x \quad \log_a 81 = \log_a 3^4 = 4$$

$a = 3$

Find the missing values:

$$5 = \log_{10} a$$

$$10^5 = a = 100000$$

$$3 = \log_2 a$$

$$2^3 = a = 8$$

## Rules for Logarithms

$$a^0 = 1 \quad \text{then} \quad \log_a 1 = 0$$

$$a^1 = a \quad \text{then} \quad \log_a a = 1$$

$$\log_a x + \log_a y = \log_a (xy)$$

$$\log_a x - \log_a y = \log_a \left(\frac{x}{y}\right)$$

$$\log_a x^n = n \log_a x$$

**Exercise 1c**

- 1**
- |          |             |
|----------|-------------|
| <b>a</b> | $3\log_7 3$ |
| <b>b</b> | 2           |
| <b>c</b> | 1           |
| <b>d</b> | 2           |
| <b>e</b> | 2           |
| <b>f</b> | 0           |
| <b>g</b> | 2           |
| <b>h</b> | 0           |

- 2**
- |          |    |
|----------|----|
| <b>a</b> | 1  |
| <b>b</b> | -2 |
| <b>c</b> | 3  |
| <b>d</b> | 0  |
| <b>e</b> | 1  |
- 3**
- |          |                 |
|----------|-----------------|
| <b>a</b> | 5               |
| <b>b</b> | 3               |
| <b>c</b> | -1              |
| <b>d</b> | 3               |
| <b>e</b> | 1               |
| <b>f</b> | 2               |
| <b>g</b> | -5              |
| <b>h</b> | -1              |
| <b>i</b> | 3               |
| <b>j</b> | $\frac{3}{2}$   |
| <b>k</b> | $11\frac{1}{2}$ |